## University of <br> South Australia

## Percentages (\%) - Worksheet

Percentages are used to compare parts of an original. A percentage is expressed by a number followed by a percentage (\%) sign and illustrates the portion considering ' 100 ' as the whole.

## Example

$20 \%$ means 20 parts of 100.
Hence, in the case of $20 \%$ discount on a price; if the price is $\$ 100$, you'd pay $\$ 20$ less. But if the price is $\$ 500$, which is $\left(5^{*} \$ 100\right)$, you'd pay $\left(5^{*} 20\right)=\$ 100$ less.

If the price is $\$ 750$ (that is $\left.7.5^{*} 100\right)^{\prime}$ you would pay $\$ 150\left(7.5^{*} 20=150\right)$ less from the price.

## Methods of calculation

As explained above, percentage is the number illustrating parts of 100 . Hence, we can write the percentage as a fraction with 100 as the denominator.
e.g., $40 \%=40 / 100$

So, if we need to calculate $40 \%$ of 500 , we can model it like this:
$\frac{40}{100} \times \frac{500}{1}=200$
Example
Calculate 35\% of 250.
$\frac{35}{100} \times \frac{250}{1}=87.5$
Note: even if the percentage is a whole number, the calculated amount can be a decimal depending on the original number.

## Calculating 'how much is the new amount'?

Imagine you are buying a shirt at $25 \%$ discount which is originally priced at $\$ 150$. How much would you pay after the discount?

These type of questions require an added step in the calculation where you find out 'how much is left' from the original amount after the discount.

## Example

As in this situation,
Discount amount:
$\frac{25}{100} \times \frac{150}{1}=37.5$

So, you would receive $\$ 37.5$ discount on the shirt. But the question is: how much would you pay? To calculate the discounted price, you need to take away the discount amount from the original price:
$\$ 150-\$ 37.5=\$ 112.5$

## Example

Your cousin has 45 cards. You give $12.5 \%$ more to him as a gift. How many cards does he have now?
Total number of cards= 45
$12.5 \%$ more were gifted, that is:
$\frac{12.5}{100} \times \frac{45}{1}=5$
5 cards more were given. Hence, he now has: $45+5=50$ cards.

## Calculating 'how much was the original amount'?

You might also be asked to calculate the original amount from the new amount, given the percentage.

## Example

You bought a novel for $\$ 25$ after a $20 \%$ off sale. What was the book's original price?
We know that the price you bought the book for is the discounted price:
Discounted amount= Original amount - Discount
If we consider the original price as x and we add the information we know, our calculation might look like this:
$25=x-20 \%$ of $x$
We can write $20 \%$ as $20 / 100$
$25=x-\frac{20}{100} x$
Which is same as, $x-\frac{20}{100} x=25$
If we solve the equation, we get:
$\frac{100 x-20 x}{100}=25$
$\frac{80 x}{100}=25$
$80 x=2500$
$x=31.25$
So, the original price of the novel was $\$ 31.25$

## One step method: converting to decimal

As we already know, a percentage can be written in a fraction form with 100 in the denominator. The next step would be converting that fraction to decimal. We already know the method to convert fractions to decimal. Please refer to the Fraction chapter for a refresher.

## Example

$20 \%=\frac{20}{100}=\frac{1}{5}=0.2$
So, if we want to calculate $20 \%$ of 200 ,
$\frac{20}{100} \times \frac{200}{1}=0.2 \times 200=40$

Another way: put the decimal point after two places from the right.
So, $20 \%=0.20$
$15 \%=0.15$
$7 \%=0.07$ (note: if the percentage is one digit, you put zero on the left to make it two places after the decimal point)

Example
Scenario 1: $25 \%$ discount on a price of $\$ 300$. Calculate the new price.
Here, the new amount would be less than the original.
Step 1: take away $25 \%$ from $100 \%$, which gives us $75 \%$
Step 2: Convert the percentage into decimal. $75 \%=0.75$
Step 3: multiply the decimal with the original amount to calculate the new amount,

$$
(\$ 300 * 0.75)=\$ 225
$$

So, the discounted price is $\$ 225$
Scenario 2: 6\% raise on salary originally $\$ 20 / \mathrm{hr}$.
Here, the new amount would be higher than the original.

Step 1: add 6\% to $100 \%$, which gives us $106 \%$
Step 2: Convert the percentage into decimal. 106\% = 1.06
Step 3: multiply the decimal with the original amount to calculate the new amount:

$$
(\$ 20 * 1.06)=\$ 21.2
$$

So, the new salary is $\$ 21.2 / \mathrm{hr}$.
The example problem in 'Calculating - how much was the original amount?' section could be solved in a simpler way if we convert the percentage into a decimal point. Here we want to calculate the original amount.

## Example

Scenario 1: 20\% discount gives you a discounted price of \$25
Here, the original amount would be more than the new amount.
Step1: take out $20 \%$ to $100 \%$, which gives us $80 \%$
Step 2: Convert the percentage into decimal. $80 \%=0.8$
Step 3: divide the new amount by the decimal to calculate the original amount: $(\$ 25 \div 0.8)=\$ 31.25$ So, the original price is $\$ 31.25$

Scenario 2: 6\% raise on salary gives you \$21.2/hr
Here, the original amount would be less than the new salary.
Step1: add 6\% to $100 \%$, which gives us $106 \%$
Step 2: Convert the percentage into decimal. 106\% = 1.06
Step 3: divide the decimal with the new amount to calculate the original amount,

$$
(\$ 21.2 \div 1.06)=\$ 20
$$

So, the new salary is $\$ 20 / \mathrm{hr}$.

## Calculating 'the percentage'?

To calculate the percentage, we need information about the original and the new amount.

## Example

A toy originally priced for $\$ 10$ is sold on special for $\$ 7$. What is the discount rate?
Step 1 is to calculate the change between the new and the original amount. Here the discount amount can be calculated by taking out the new price from the original price.

Discount amount $=\$ 10-\$ 7=\$ 3$

As we know, percentage is the portion of 100, we need to calculate the discount amount for 100.

Discount percentage $=\frac{3}{10} \times \frac{100}{1}=30 \%$

## Practice Exercises

## Question 1

Calculate the portion of the original number depending on the given percentages:

| No. | Original number | Percentage | Answer |
| :--- | :--- | :--- | :--- |
| 1 | 935 | $10 \%$ |  |
| 2 | 200 | $2.5 \%$ |  |
| 3 | 75 | $40 \%$ |  |
| 4 | 732 | $35 \%$ |  |
| 5 | 340 | $27 \%$ |  |

## Question 2

Change the following percentages into decimal points,

| No. | Percentage | Decimal |
| :--- | :--- | :--- |
| 1 | $93 \%$ |  |
| 2 | $2 \%$ |  |
| 3 | $115 \%$ |  |
| 4 | $27 \%$ |  |
| 5 | $2.5 \%$ |  |

## Question 3

There is a $30 \%$ sale going on in a branded store on shoes. If you choose a pair of shoes originally priced $\$ 250$, how much is the discount?

## Question 4

For the new financial year, an employee has received a $2.5 \%$ pay rise. If the previous rate was $\$ 23.97$ per hour, what is their new rate?

## Question 5

A student scored 42 out of 50 in the first math test and scored 48 out of 50 on the second. By what percentage has the student's result improved?

## Question 6

You are looking for a new house for rent and the rates have increased by $20 \%$. You are about to rent a house for $\$ 320 /$ week. How much was the earlier rent for the house?

