



University of
South Australia

ENR116 Engineering Materials

Module 4 Non-metals and Corrosion

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Fibre-reinforced composites



Intended Learning Outcomes

At the end of this section, students will be able to:-

- Describe the **types** of **fibre-reinforced** composites.
- Explain the effects of **fibre alignment** on the **mechanical properties** of the composite.



Fibre composites

Particle-reinforced

Fibre-reinforced

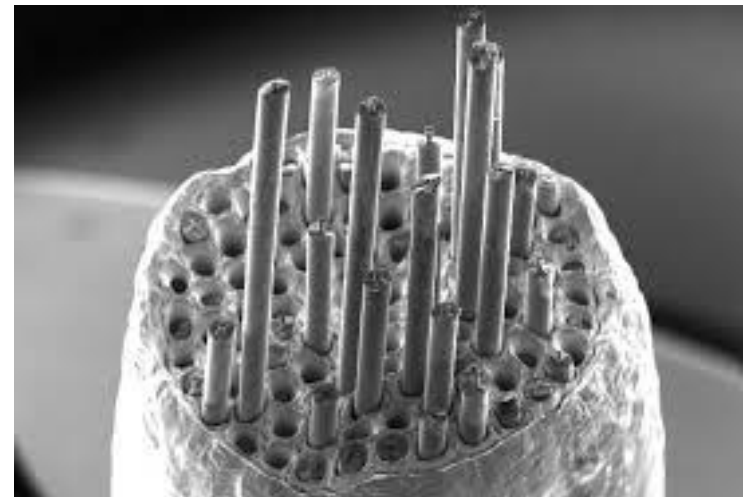
Structural

Dispersed phase is in the form of a fibre:

Technologically, the most important of the composites.

May be continuous or
discontinuous

Design goals of fibre-reinforced
composites include high strength
and/or stiffness on a weight basis.





Fibre composites

Particle-reinforced

Fibre-reinforced

Structural

Mechanical characteristics depend on:

- The properties of the fibre.
- The degree to which an applied load is transmitted to the fibres by the matrix phase.
- The magnitude of the **interfacial bond** between the fibre and matrix

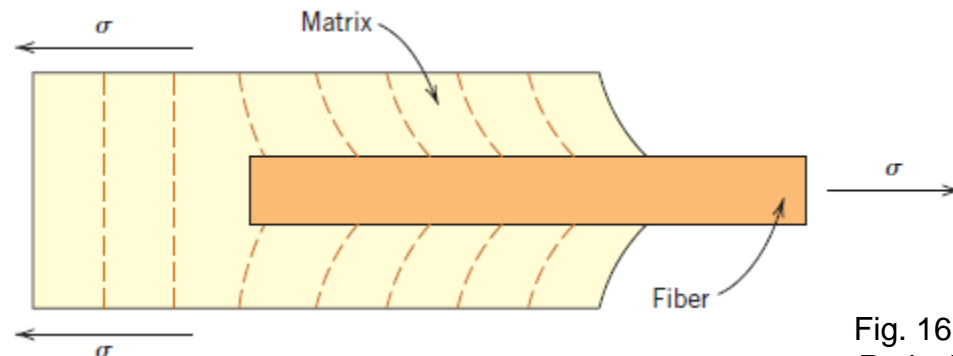


Fig. 16.06, Callister &
Rethwisch 8e.



Critical fibre length

Particle-reinforced

Fibre-reinforced

Structural

Critical fibre length; l_c

$$l_c = \frac{\sigma_f^* d}{2\tau_c}$$

l_c , critical length is dependent on the:

- d - fibre diameter
- σ_f^* - ultimate (or tensile) strength
- τ_c - fibre-matrix bond strength

For a number of glass and carbon fibre-matrix combinations, l_c is in the order of 1 mm (between 20 and 150 times the fibre diameter).



Continuous vs. discontinuous fibres



$$l \gg l_c$$

$(l > 15 l_c)$ - continuous
(Below this, 'discontinuous')

Longer fibre - more
effective reinforcement!

Fig. 16.07, Callister
& Rethwisch 8e.

For a significant improvement in strength the fibres must be
continuous.



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Fiber Alignment



Continuous and Aligned Fibres



Continuous and Aligned Fibre Composites, under a longitudinal load:

Mechanical properties depend on:

- The phase **volume fractions**.
- The **direction** in which stress or load is applied.

Properties of a composite having its **fibres aligned** are highly **anisotropic** (dependent on the direction in which they are measured).



Continuous and Aligned Fibres

Particle-reinforced

Fibre-reinforced

Structural

Composite failure is
not catastrophic:

Fibres do not fracture
at the same time.

Shortened fibres after
fracture still have a
reinforcement effect



Fibre reinforcement

Particle-reinforced

Fibre-reinforced

Structural

Consider the **elastic** behaviour of a continuous and oriented fibrous composite loaded in the direction of **fibre alignment**.

Assuming that the fibre-matrix interfacial bond is very good, total load sustained by the composite:

$$F_c = F_m + F_f$$

Eqn. 1

F_c - force carried by the composite

F_m - force carried by the matrix

F_f - force carried by the fibre phase



Fibre reinforcement

Particle-reinforced

Fibre-reinforced

Structural

Since $F = \sigma A$,

$$\sigma_c A_c = \sigma_m A_m + \sigma_f A_f$$

$V_f = A_f / A_c$ volume fraction of
the fibre phase.

$$\sigma_c = \sigma_m \frac{A_m}{A_c} + \sigma_f \frac{A_f}{A_c}$$

Eqn. 2

$$\sigma_c = \sigma_m V_m + \sigma_f V_f$$

Eqn. 3



Fibre reinforcement

Particle-reinforced

Fibre-reinforced

Structural

Isostrain state means that:

$$\epsilon_c = \epsilon_m = \epsilon_f$$

Divide Eqn. 3 (for σ_c) by the strain:

$$\frac{\sigma_c}{\epsilon_c} = \frac{\sigma_m}{\epsilon_m} V_m + \frac{\sigma_f}{\epsilon_f} V_f$$

If composite, matrix, and fibre deformations are all elastic, then:

$$\frac{\sigma_c}{\epsilon_c} = E_c$$



Longitudinal loading

Particle-reinforced

Fibre-reinforced

Structural

Modulus of elasticity of a continuous and aligned fibrous composite *in the direction of alignment* (*longitudinal direction*):

$$E_{cl} = E_m V_m + E_f V_f$$

$$\text{Or.... } E_{cl} = E_m(1 - V_f) + E_f V_f$$

For longitudinal loading the ratio of the load carried by the fibres to that carried by the matrix is:

$$\frac{F_f}{F_m} = \frac{E_f V_f}{E_m V_m}$$



Transverse loading

Particle-reinforced

Fibre-reinforced

Structural

Elastic Behaviour - Transverse Loading

Load is applied at a **90° angle** to the direction of fibre alignment.

For this situation the stress to which the composite as well as both phases are exposed is the same:

$$\sigma_c = \sigma_m = \sigma_f = \sigma$$



Transverse loading

Particle-reinforced

Fibre-reinforced

Structural

This is an **isostress state**:

$$\epsilon_c = \epsilon_m V_m + \epsilon_f V_f$$

and, as

$$\epsilon = \sigma / E$$

$$\frac{\sigma}{E_{ct}} = \frac{\sigma}{E_m} V_m + \frac{\sigma}{E_f} V_f$$

Eqn. 4

E_{ct} is the modulus of elasticity in the transverse direction.



Transverse loading

Particle-reinforced

Fibre-reinforced

Structural

$$\frac{\sigma}{E_{ct}} = \frac{\sigma}{E_m} V_m + \frac{\sigma}{E_f} V_f$$

Eqn. 4

Dividing through by σ and reducing:

$$E_{ct} = \frac{E_m E_f}{V_m E_f + V_f E_m} = \frac{E_m E_f}{(1 - V_f) E_f + V_f E_m}$$



Longitudinal Tensile Strength

Particle-reinforced

Fibre-reinforced

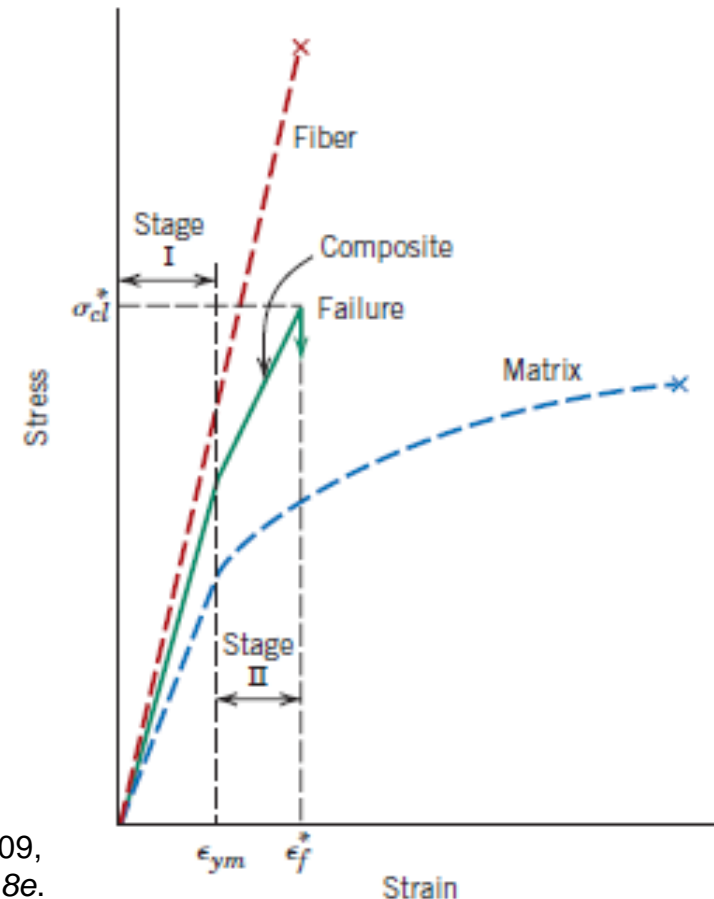
Structural

Longitudinal Tensile Strength:

Strength is normally taken as the maximum stress.

$$\sigma_{cl}^* = \sigma_m' (1 - V_f) + \sigma_f^* V_f$$

σ_m is the stress in the matrix at fibre failure.



Adapted from Fig. 16.09,
Callister & Rethwisch 8e.



Transverse Tensile Strength

Particle-reinforced

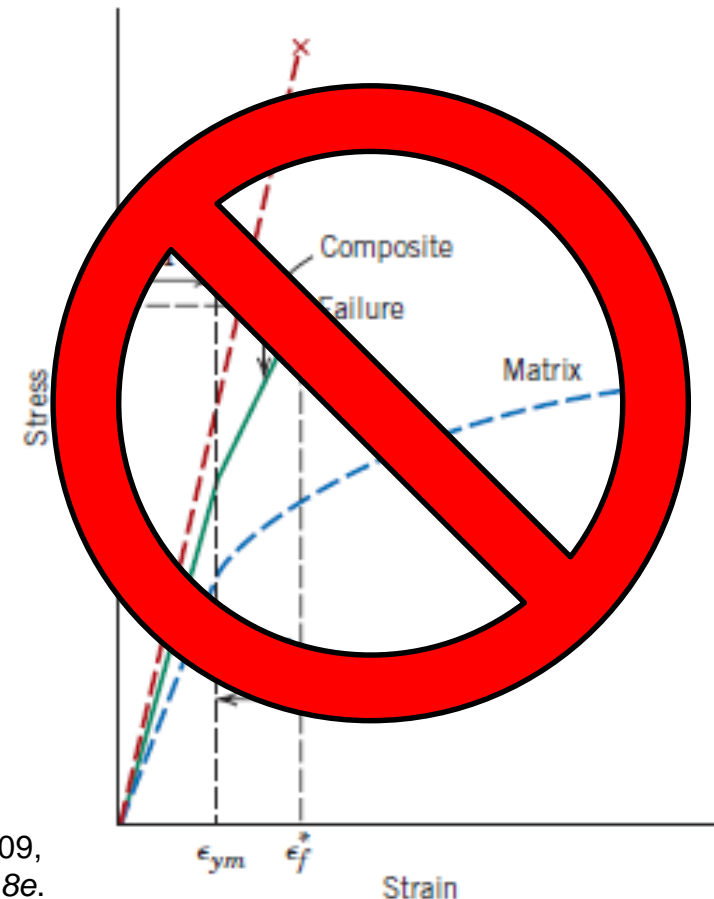
Fibre-reinforced

Structural

Transverse Tensile Strength:

Will be ***much smaller*** than the longitudinal strength.

Important factors include;
properties of both the fibre and matrix,
the fibre-matrix bond strength,
and the presence of voids.



Adapted from Fig. 16.09,
Callister & Rethwisch 8e.



Summary

- Fibre-reinforced composites can be:
 - continuous and aligned
 - discontinuous and aligned
 - discontinuous and random
- The improved mechanical properties of composites are influenced by the matrix-fibre bond strength and the fibre direction.



Thank you